



# Introduction to Trigonometry with Applications

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APPLICATION EXAMPLE: ANALYSIS FOR ERROR IN POSITIONING OF  
TIP OF TWO-LINK ROBOT

PANOS S. SHIAKOLAS

DEPARTMENT OF MECHANICAL AND AEROSPACE ENGINEERING

COLLEGE OF ENGINEERING

UNIVERSITY OF TEXAS AT ARLINGTON



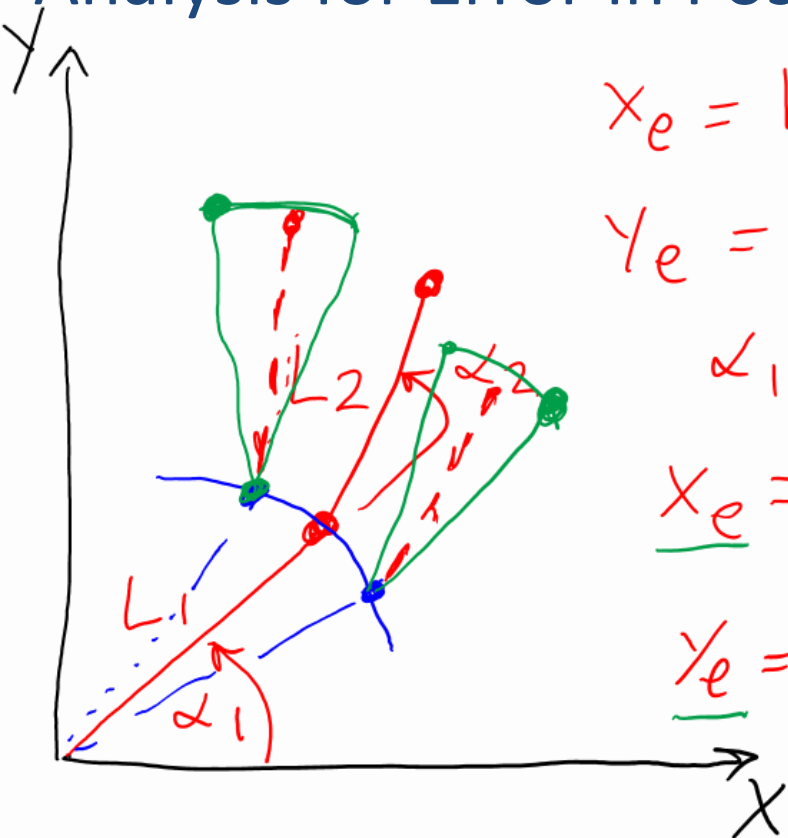
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# Application Example

## Analysis for Error in Positioning of Tip of Two-Link Robot



$$x_e = L_1 \cos(\alpha_1) + L_2 \cos(\alpha_1 + \alpha_2)$$

$$y_e = L_1 \sin(\alpha_1) + L_2 \sin(\alpha_1 + \alpha_2)$$

$$\alpha_1 \rightarrow \pm \Delta\alpha \quad \alpha_2 \rightarrow \pm \Delta\alpha$$

$$\underline{x_e} = L_1 \cos(\alpha_1 \pm \Delta\alpha) + L_2 \cos(\alpha_1 \pm \Delta\alpha + \alpha_2 \pm \Delta\alpha)$$

$$\underline{y_e} = L_1 \sin(\alpha_1 \pm \Delta\alpha) + L_2 \sin(\alpha_1 \pm \Delta\alpha + \alpha_2 \pm \Delta\alpha)$$

$L_1$	$\&$	$L_2$	$\alpha_1$	$\alpha_2$	$\alpha_2 \pm \Delta\alpha$
50 mm		40 mm	30°	45°	$\frac{\Delta\alpha}{10}$