

Categorical Data and One-Hot-Encoding



Logistic Regression Optimization

Regularized

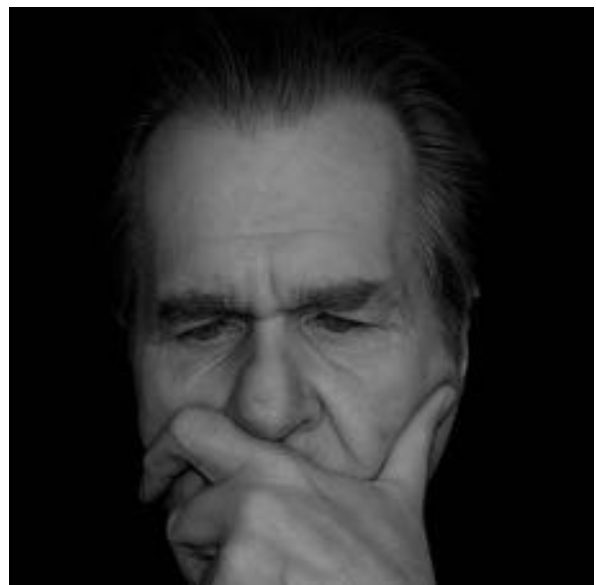
✓ **Logistic Regression:** Learn mapping (\mathbf{w}) that minimizes logistic loss on training data with a regularization term

$$\min_{\mathbf{w}} \sum_{i=1}^n \overbrace{\ell_{0/1} \left(y^{(i)} \cdot \mathbf{w}^\top \mathbf{x}^{(i)} \right)}^{\text{Training LogLoss}} + \overbrace{\lambda ||\mathbf{w}||_2^2}^{\text{Model Complexity}}$$

Data is assumed to be **numerical!**

Similar story for linear regression and many other methods

Raw Data is Sometimes Numeric



Images

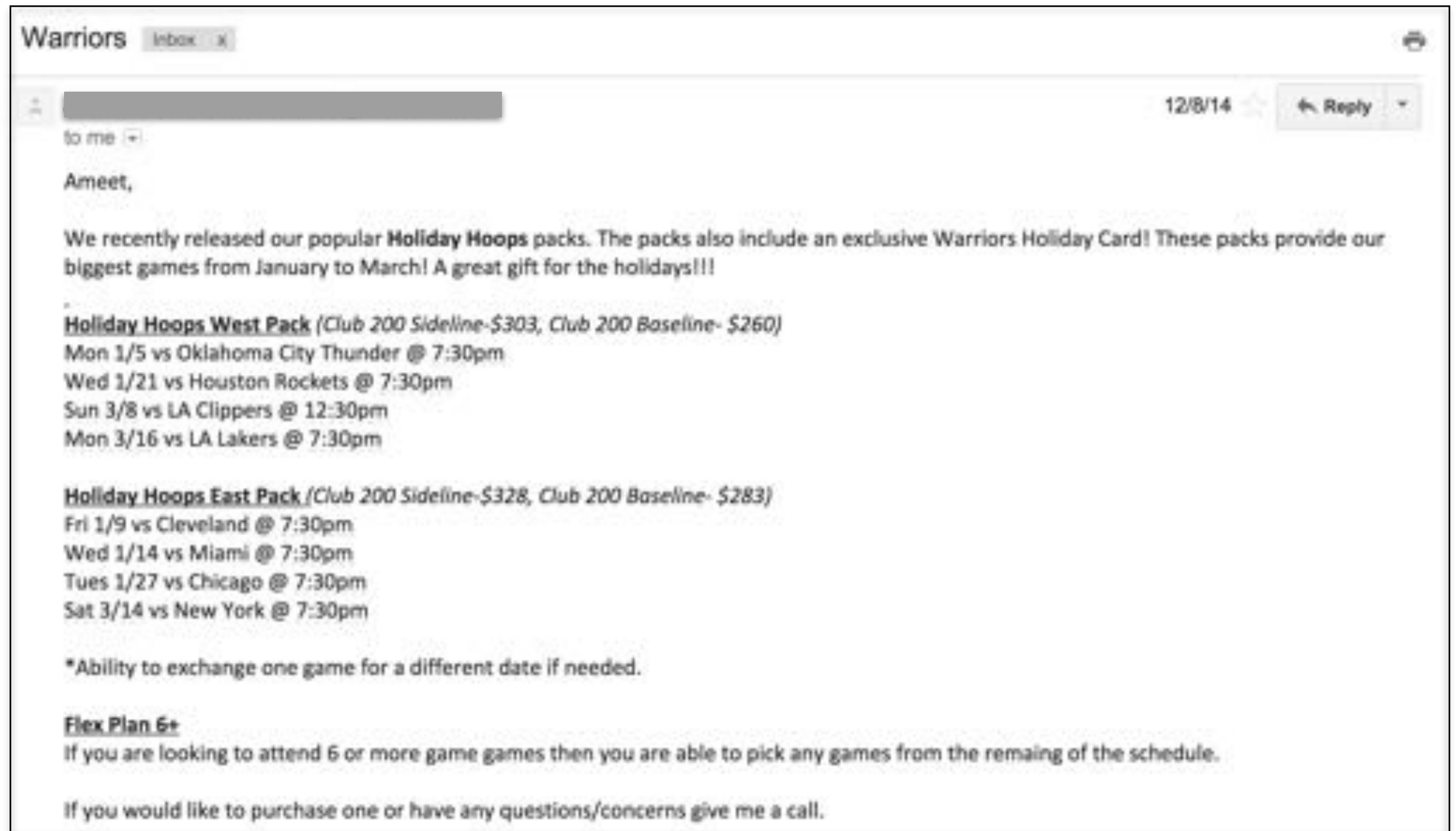


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|------|----|------|----|
| | ★ | ★★★★ | |
| | ★ | ★★★ | ★★ |
| ★★★★ | | | ★ |
| ★ | | | ★★ |
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| ★★★★ | ★★ | | |

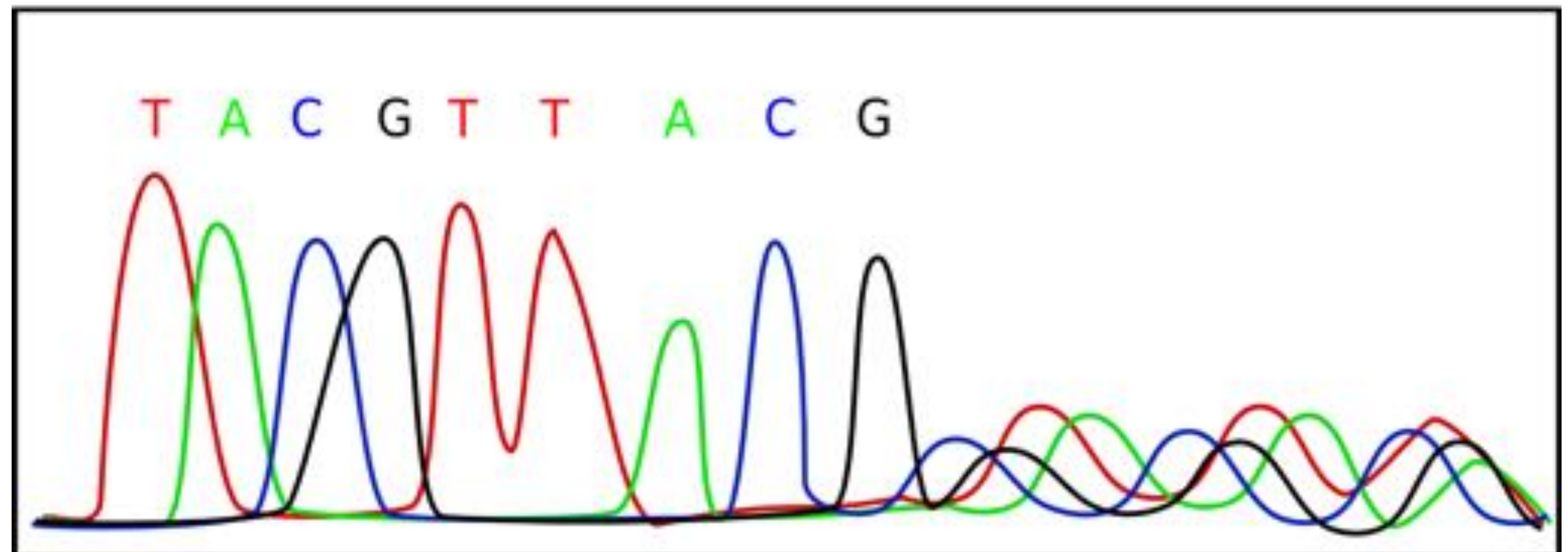
User Ratings

Raw Data is Often Non-Numeric

Email



Genomic
Data



Web hypertext

```
1 <!DOCTYPE html PUBLIC "-//W3C//DTD
  XHTML 1.0 Transitional//EN"
2 "http://www.w3.org/TR/xhtml1/DTD/
  xhtml1-transitional.dtd">
3
4 <html xmlns="http://www.w3.org/1999/
  xhtml">
5   <head>
6     <meta http-equiv="Content-
  Type" content=
7     "text/html; charset=us-
  ascii" />
8     <script type="text/
  javascript">
9       function reDo() {top.
  location.reload();}
10      if (navigator.appName ==
  'Netscape') {top.onresize = reDo;}
11      dom=document.
  getElementById;
12    </script>
13  </head>
14  <body>
15  </body>
16 </html>
```

Raw Data is Often Non-Numeric

Example: Click-through Rate Prediction

- User features: Gender, Nationality, Occupation, ...
- Advertiser / Publisher: Industry, Location, ...
- Ad / Publisher Site: Language, Text, Target Audience, ...

How to Handle Non-Numeric Features?

Option 1: Use methods that support these features

- Some methods, e.g., Decision Trees, Naive Bayes, naturally support non-numerical features
- However, this limits our options

Option 2: Convert these features to numeric features

- Allows us to use a wider range of learning methods
- How do we do this?

Types of Non-Numeric Features

Categorical Feature

- Has two or more categories
- No intrinsic ordering to the categories
- E.g., Gender, Country, Occupation, Language

Ordinal Feature

- Has two or more categories
- Intrinsic ordering, but no consistent spacing between categories, i.e., all we have is a relative ordering
- Often seen in survey questions, e.g., “Is your health poor, reasonable, good, excellent”

Non-Numeric \Rightarrow Numeric

One idea: Create single numerical feature to represent non-numeric one

Ordinal Features:

- Health categories = {'poor', 'reasonable', 'good', 'excellent'}
- 'poor' = 1, 'reasonable' = 2, 'good' = 3, 'excellent' = 4

We can use a single numerical feature that preserves this ordering ... but ordinal features only have an ordering and we introduce a degree of closeness that didn't previously exist

Non-Numeric \Rightarrow Numeric

One idea: Create single numerical feature to represent non-numeric one

Categorical Features:

- Country categories = {'ARG', 'FRA', 'USA'}
- 'ARG' = 1, 'FRA' = 2, 'USA' = 3
- Mapping implies FRA is between ARG and USA

Creating single numerical feature introduces relationships between categories that don't otherwise exist

Non-Numeric \Rightarrow Numeric

Another idea (One-Hot-Encoding): Create a 'dummy' feature for each category

Categorical Features:

- Country categories = {'ARG', 'FRA', 'USA'}
- We introduce one new dummy feature for each category
- 'ARG' \Rightarrow [1 0 0], 'FRA' \Rightarrow [0 1 0], 'USA' \Rightarrow [0 0 1]

Creating dummy features doesn't introduce spurious relationships

Computing and Storing OHE Features



Example: Categorical Animal Dataset

Features:

- Animal = {'bear', 'cat', 'mouse'}
- Color = {'black', 'tabby'}
- Diet (optional) = {'mouse', 'salmon'}

Datapoints:

- A1 = ['mouse', 'black', -]
- A2 = ['cat', 'tabby', 'mouse']
- A3 = ['bear', 'black', 'salmon']

How can we create OHE features?

Step 1: Create OHE Dictionary

Features:

- Animal = {'bear', 'cat', 'mouse'}
- Color = {'black', 'tabby'}
- Diet = {'mouse', 'salmon'}

7 dummy features in total

- 'mouse' category distinct for Animal and Diet features

OHE Dictionary: Maps each category to dummy feature

- (Animal, 'bear') \Rightarrow 0
- (Animal, 'cat') \Rightarrow 1
- (Animal, 'mouse') \Rightarrow 2
- (Color, 'black') \Rightarrow 3
- ...

Step 2: Create Features with Dictionary

Datapoints:

- A1 = ['mouse', 'black', -]
- A2 = ['cat', 'tabby', 'mouse']
- A3 = ['bear', 'black', 'salmon']

OHE Features:

- Map non-numeric feature to its binary dummy feature
- E.g., A1 = [0, 0, 1, 1, 0, 0, 0]



OHE Dictionary: Maps each category to dummy feature

- (Animal, 'bear') \Rightarrow 0
- (Animal, 'cat') \Rightarrow 1
- (Animal, 'mouse') \Rightarrow 2
- (Color, 'black') \Rightarrow 3
- ...

Step 2: Create Features with Dictionary

Datapoints:

- A1 = ['mouse', 'black', -]
- A2 = ['cat', 'tabby', 'mouse']
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OHE Features:

- Map non-numeric feature to its binary dummy feature
- E.g., A1 = [0, 0, 1, 1, 0, 0, 0]



OHE Dictionary: Maps each category to dummy feature

- (Animal, 'bear') \Rightarrow 0
- (Animal, 'cat') \Rightarrow 1
- (Animal, 'mouse') \Rightarrow 2
- (Color, 'black') \Rightarrow 3
- ...

OHE Features are Sparse

For a given categorical feature only a single OHE feature is non-zero — can we take advantage of this fact?

Dense representation: Store all numbers

- E.g., $A1 = [0, 0, 1, 1, 0, 0, 0]$

Sparse representation: Store indices / values for non-zeros

- Assume all other entries are zero
- E.g., $A1 = [(2,1), (3,1)]$

Sparse Representation

Example: Matrix with 10M observation and 1K features

- Assume 1% non-zeros

Dense representation: Store all numbers

- Store $10\text{M} \times 1\text{K}$ entries as doubles \Rightarrow 80GB storage

Sparse representation: Store indices / values for non-zeros

- Store value and location for non-zeros (2 doubles per entry)
- 50× savings in storage!
- We will also see computational saving for matrix operations

Feature Hashing



Non-Numeric \Rightarrow Numeric

One-Hot-Encoding: Create a 'dummy' feature for each category

Creating dummy features doesn't introduce spurious relationships

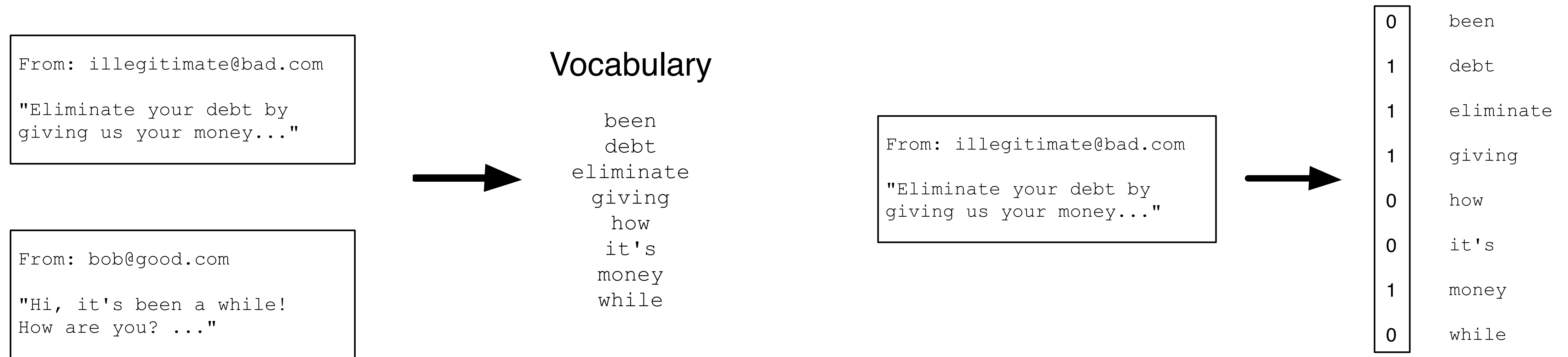
Dummy features can drastically increase dimensionality

- Number of dummy features equals number of categories!

Issue with CTR prediction data

- Includes many names (of products, advertisers, etc.)
- Text from advertisement, publisher site, etc.

“Bag of Words” Representation



Represent each document with a vocabulary of words

Over 1M words in English [Global Language Monitor, 2014]

We sometimes consider bigrams or adjacent words (similar idea to quadratic features)

High Dimensionality of OHE

Statistically: Inefficient learning

- We generally need bigger n when we have bigger d (though in distributed setting we often have very large n)
- We will have many non-predictive features

Computationally: Increased communication

- Linear models have parameter vectors of dimension d
- Gradient descent communicates the parameter vector to all workers at each iteration

How Can We Reduce Dimension?

One Option: Discard rare features

- Might throw out useful information (rare \neq uninformative)
- Must first compute OHE features, which is expensive

Another Option: Feature hashing

Can view as an unsupervised
learning preprocessing step



- Use hashing principles to reduce feature dimension
- Obviates need to compute expensive OHE dictionary
- Preserves sparsity
- Theoretical underpinnings

High-Level Idea

Hash tables are an efficient data structure for data lookup, and hash functions also useful in cryptography

Hash Function: Maps an object to one of m buckets

- Should be efficient and distribute objects across buckets

In our setting, objects are feature categories

- We have fewer buckets than feature categories
- Different categories will ‘collide’, i.e., map to same bucket
- Bucket indices are hashed features

Feature Hashing Example

Datapoints: 7 feature categories



- $A1 = [\text{'mouse'}, \text{'black'}, -]$
- $A2 = [\text{'cat'}, \text{'tabby'}, \text{'mouse'}]$
- $A3 = [\text{'bear'}, \text{'black'}, \text{'salmon'}]$

Hash Function: $m = 4$

- $H(\text{Animal}, \text{'mouse'}) = 3$
- $H(\text{Color}, \text{'black'}) = 2$

Hashed Features:

- $A1 = [0\ 0\ 1\ 1]$

Feature Hashing Example

Datapoints: 7 feature categories

- $A1 = [\text{'mouse'}, \text{'black'}, -]$
- • $A2 = [\text{'cat'}, \text{'tabby'}, \text{'mouse'}]$
- $A3 = [\text{'bear'}, \text{'black'}, \text{'salmon'}]$

Hashed Features:

- $A1 = [0\ 0\ 1\ 1]$
- $A2 = [2\ 0\ 1\ 0]$

Hash Function: $m = 4$

- $H(\text{Animal}, \text{'mouse'}) = 3$
- $H(\text{Color}, \text{'black'}) = 2$
- $H(\text{Animal}, \text{'cat'}) = 0$
- $H(\text{Color}, \text{'tabby'}) = 0$
- $H(\text{Diet}, \text{'mouse'}) = 2$

Feature Hashing Example

Datapoints: 7 feature categories

- $A1 = [\text{'mouse'}, \text{'black'}, -]$
- $A2 = [\text{'cat'}, \text{'tabby'}, \text{'mouse'}]$
- • $A3 = [\text{'bear'}, \text{'black'}, \text{'salmon'}]$

Hashed Features:

- $A1 = [0\ 0\ 1\ 1]$
- $A2 = [2\ 0\ 1\ 0]$
- $A3 = [1\ 1\ 1\ 0]$

Hash Function: $m = 4$

- $H(\text{Animal}, \text{'mouse'}) = 3$
- $H(\text{Color}, \text{'black'}) = 2$
- $H(\text{Animal}, \text{'cat'}) = 0$
- $H(\text{Color}, \text{'tabby'}) = 0$
- $H(\text{Diet}, \text{'mouse'}) = 2$
- $H(\text{Animal}, \text{'bear'}) = 0$
- $H(\text{Color}, \text{'black'}) = 2$
- $H(\text{Diet}, \text{'salmon'}) = 1$

Why Is This Reasonable?

Hash features have nice theoretical properties

- Good approximations of inner products of OHE features under certain conditions
- Many learning methods (including linear / logistic regression) can be viewed solely in terms of inner products

Good empirical performance

- Spam filtering and various other text classification tasks

Hashed features are a reasonable alternative for OHE features

Distributed Computation

```
trainHash = train.map(applyHashFunction)  
                  .map(createSparseVector)
```

Step 1: Apply hash function on raw data

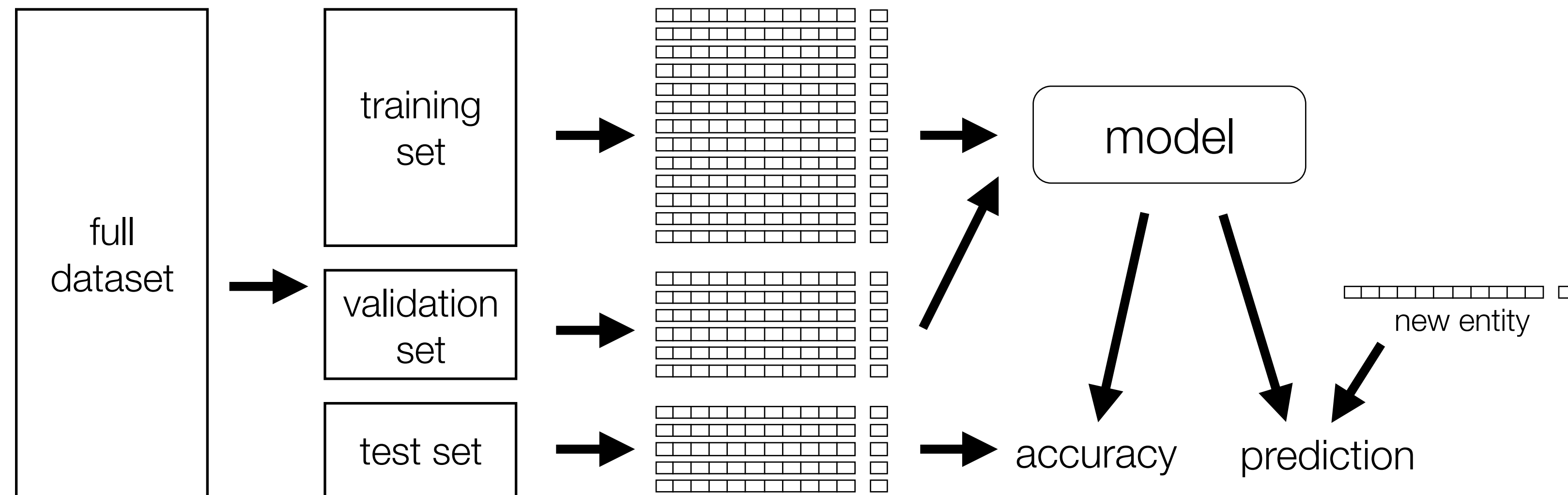
- Local computation and hash functions are usually fast
- No need to compute OHE features or communication

Step 2: Store hashed features in sparse representation

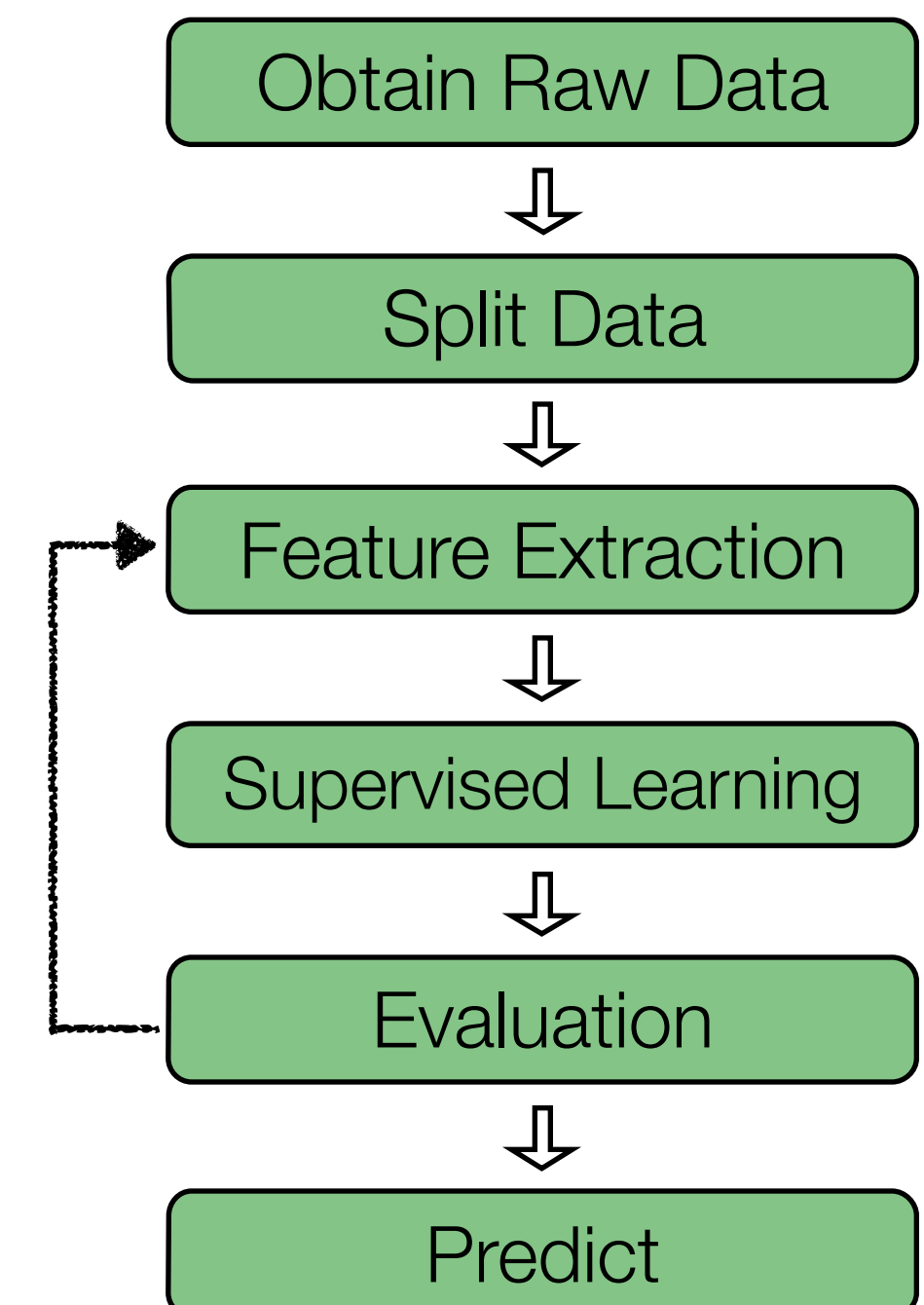
- Local computation
- Saves storage and speeds up computation

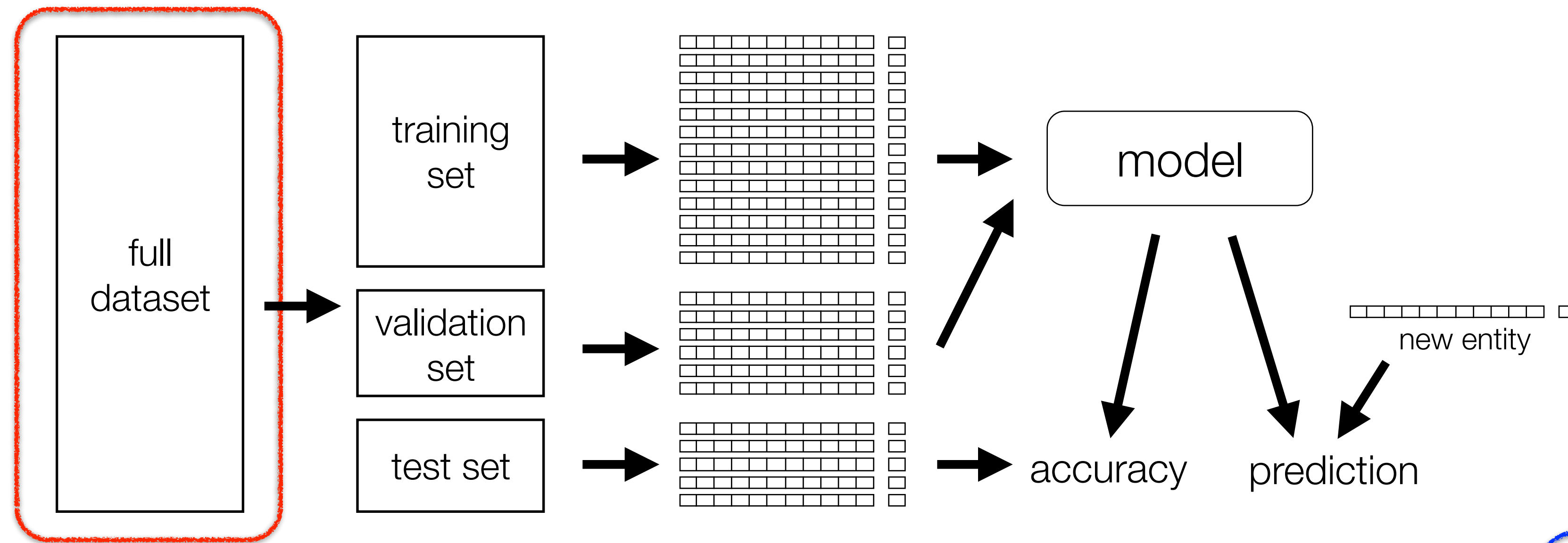
CTR Prediction Pipeline / Lab Preview





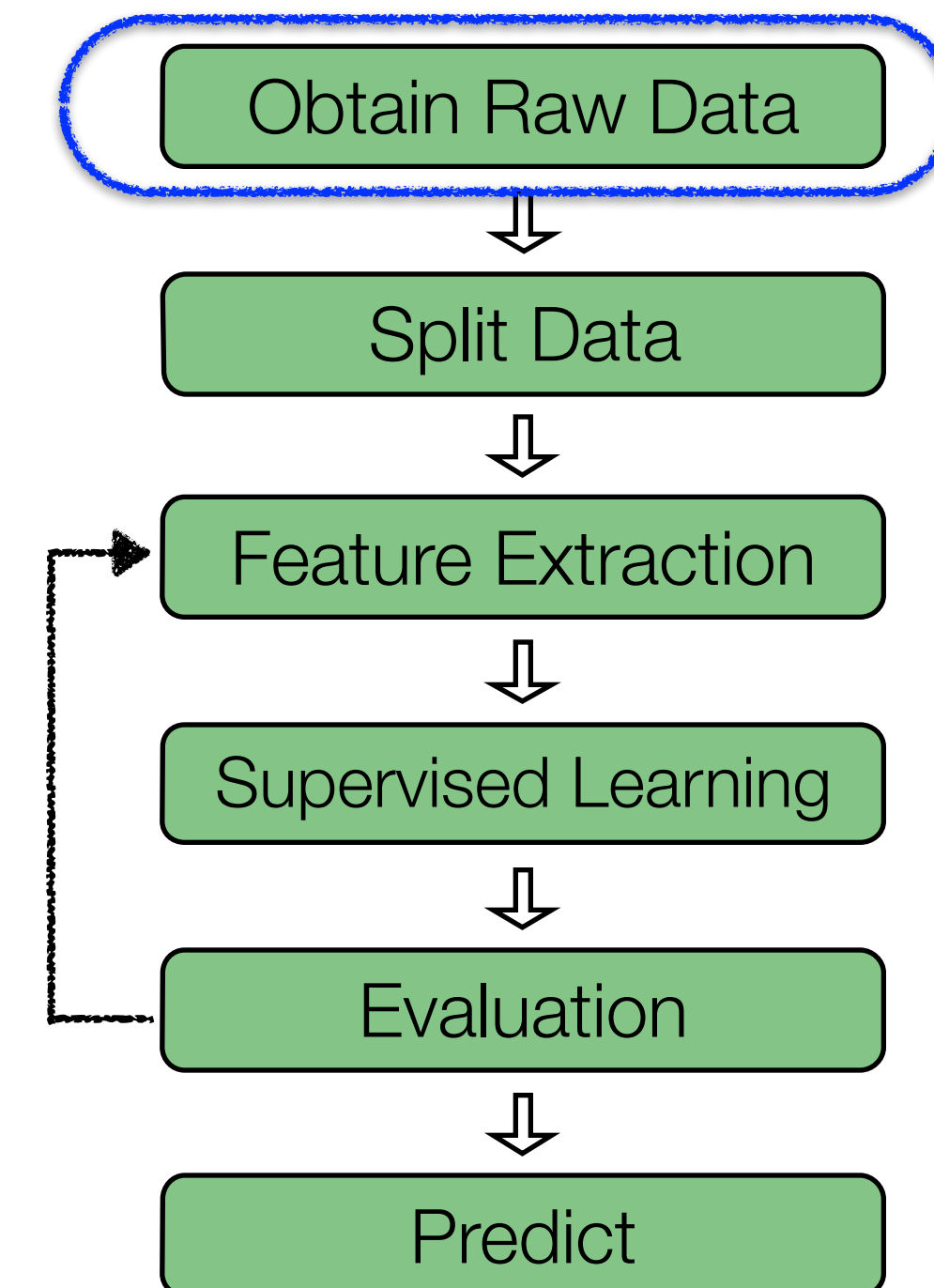
Goal: Estimate $\mathbb{P}(\text{click} \mid \text{user, ad, publisher info})$
Given: Massive amounts of labeled data

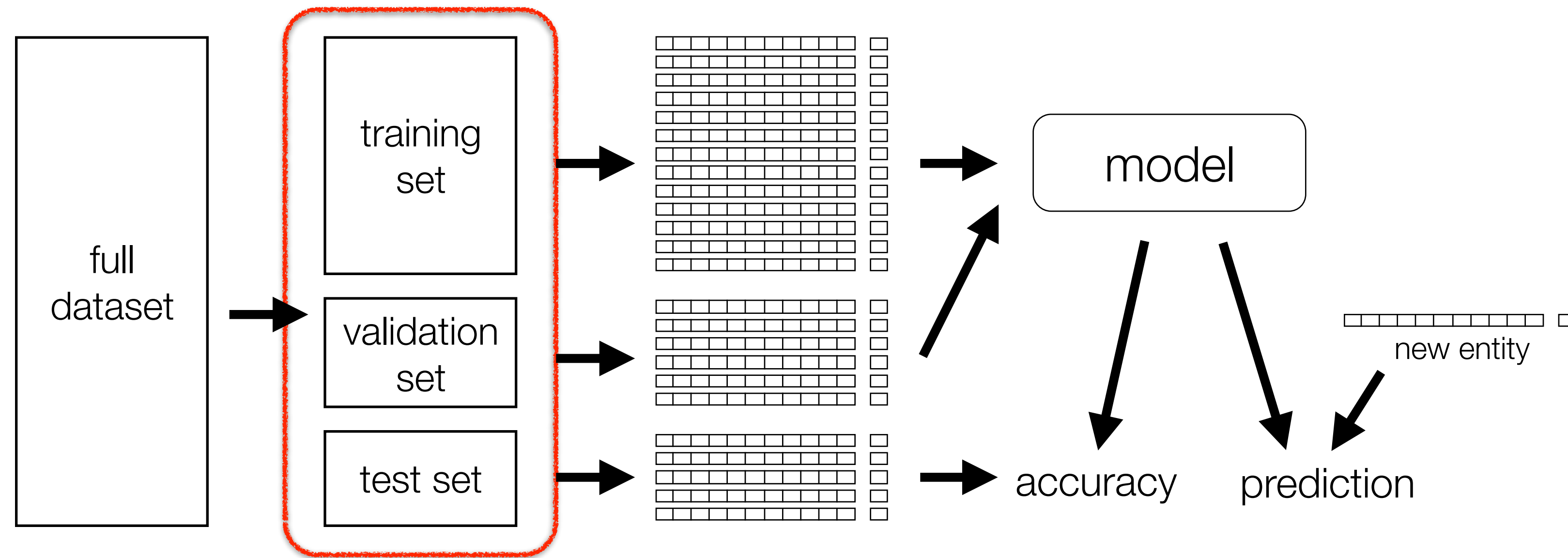




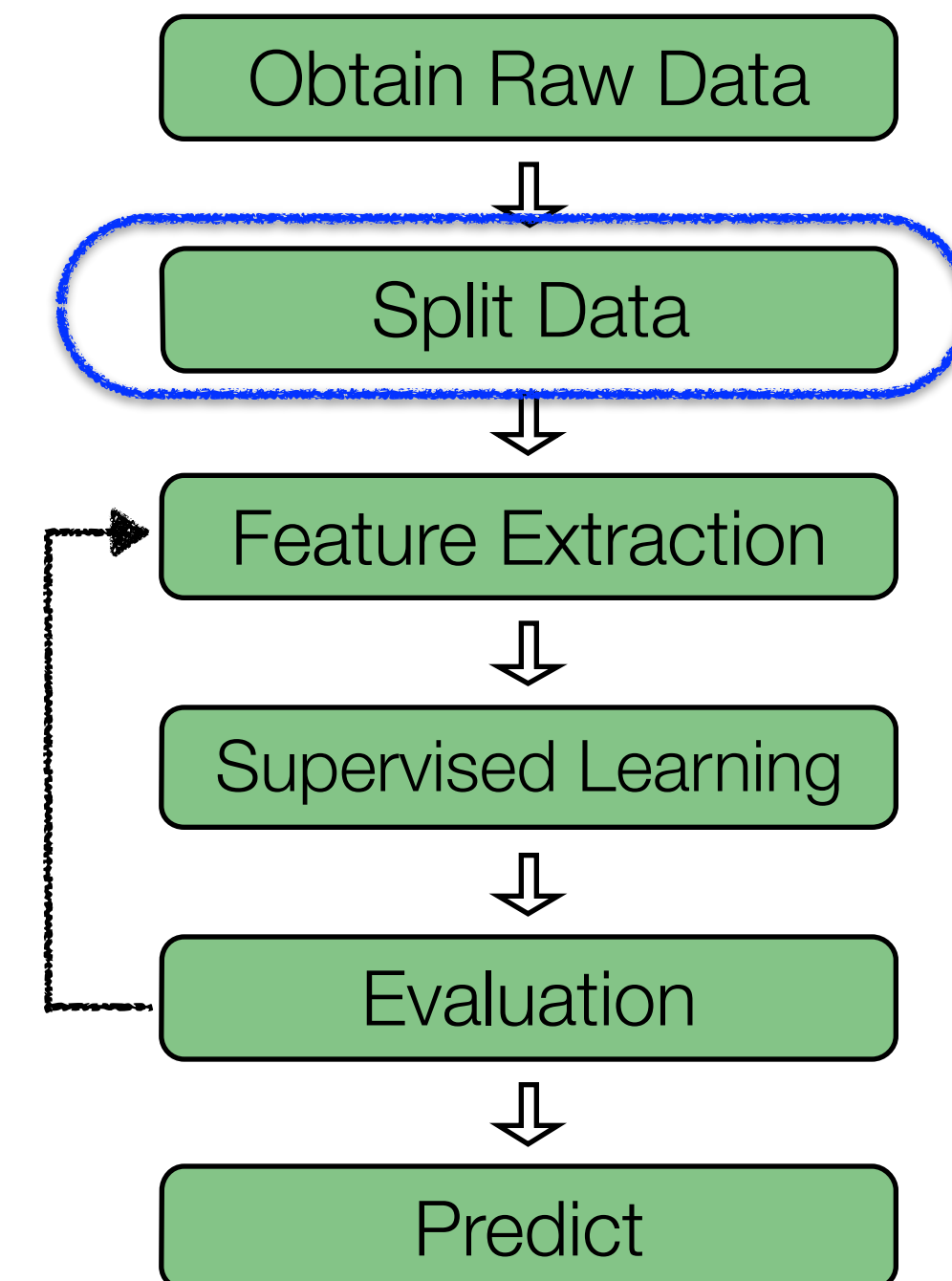
Raw Data: Criteo Dataset from Kaggle competition

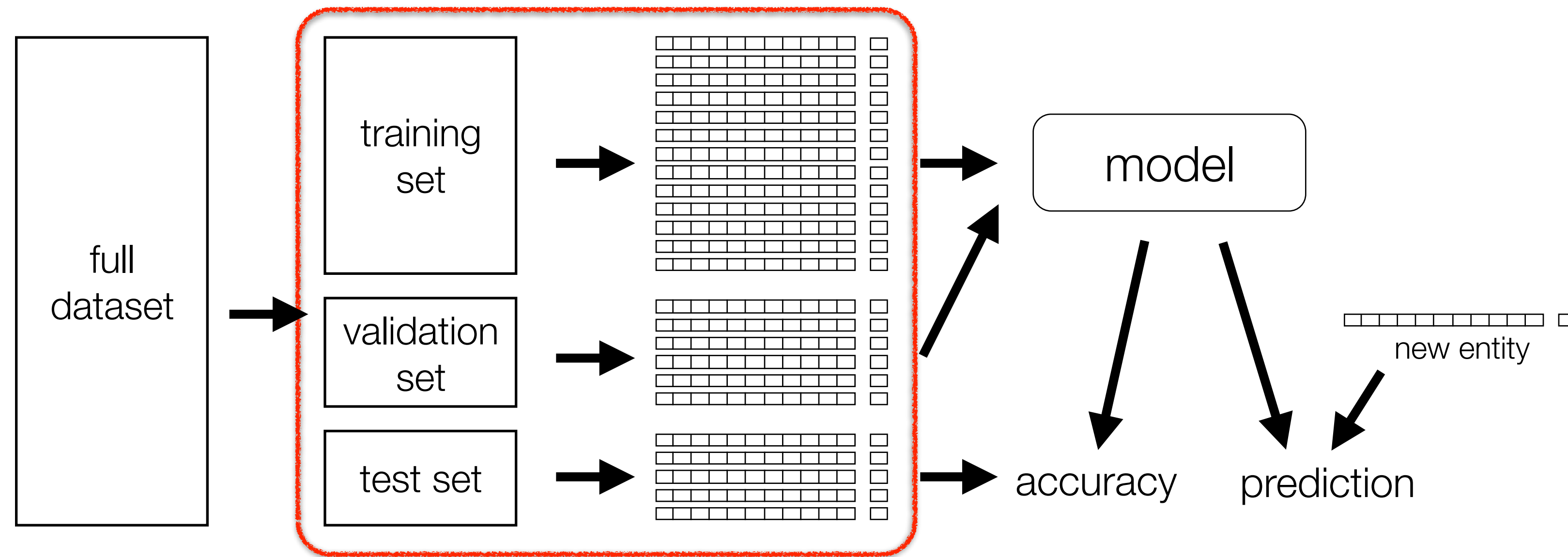
- We'll work with subsample of larger CTR dataset
- 39 masked user, ad and publisher features
- Full Kaggle dataset has 33M distinct categories (and this dataset is a small subset of Criteo's actual data)





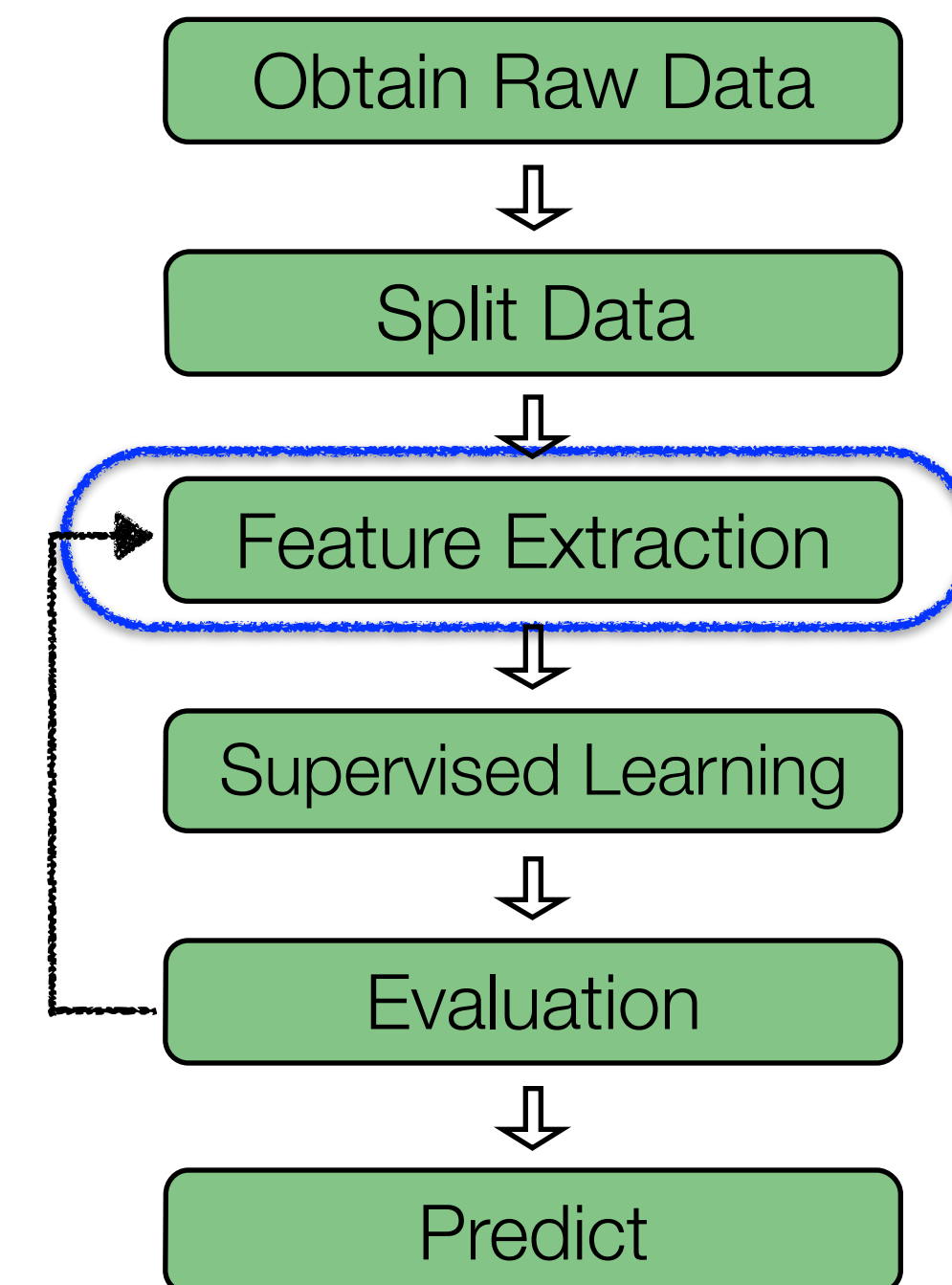
Split Data: Create training, validation, and test sets

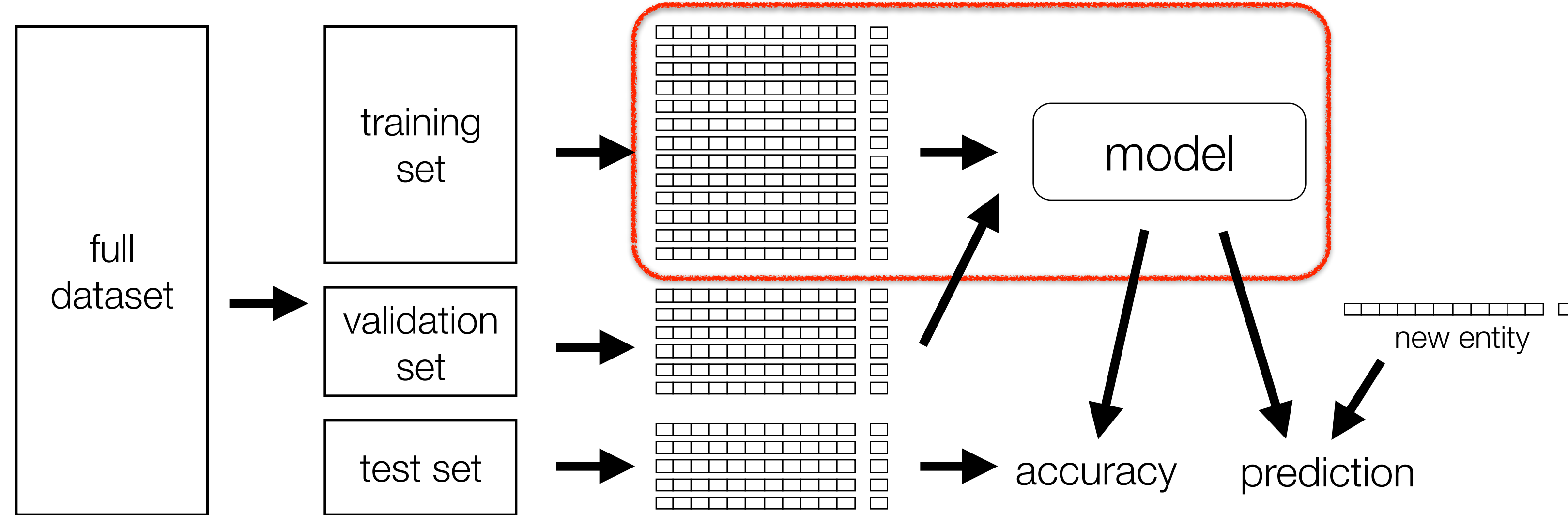




Feature Extraction: One-hot-encoding and feature hashing

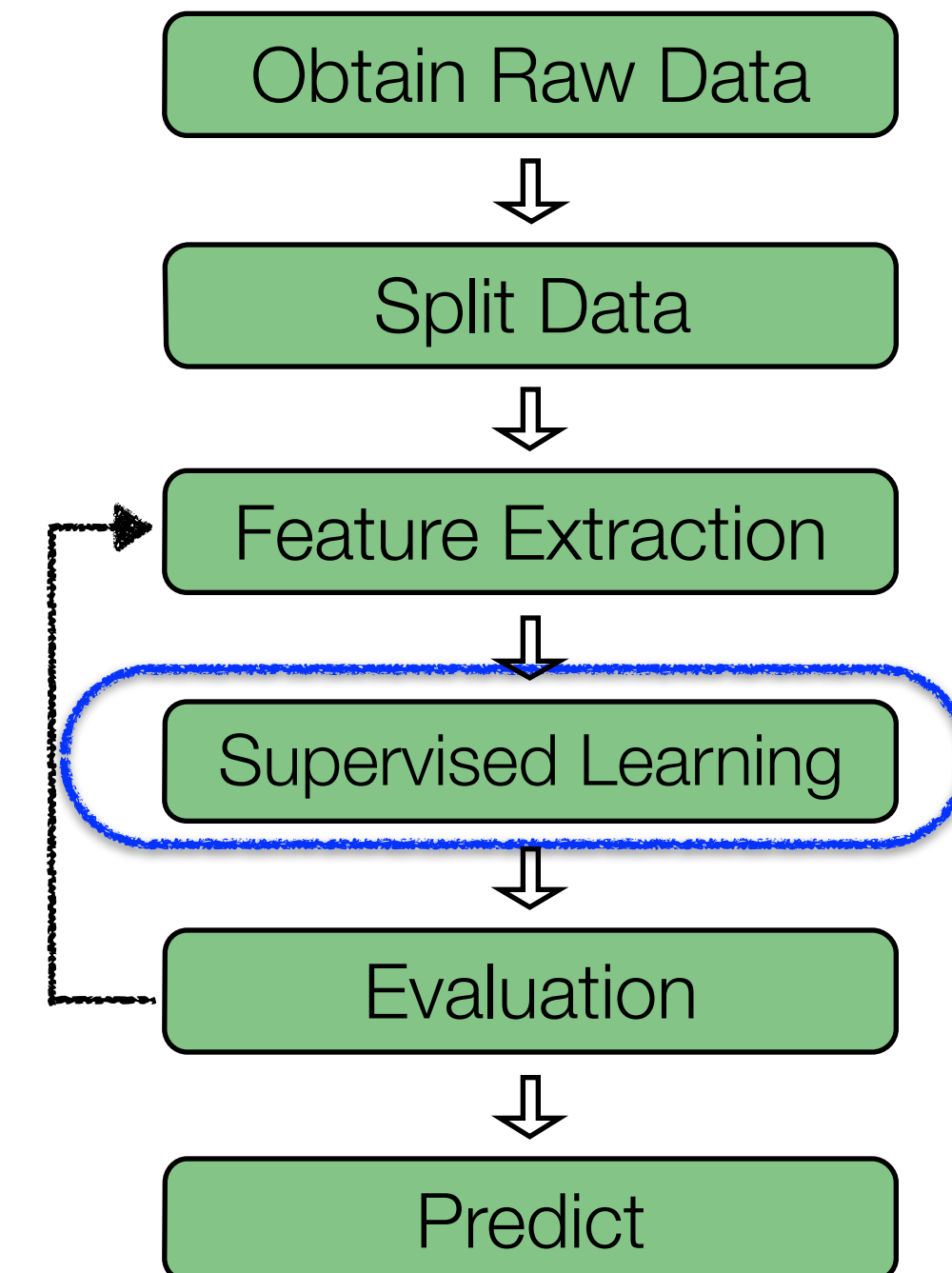
- We'll use a sparse data representation
- We'll visualize feature frequency
- Feature extraction is the main focus of this lab

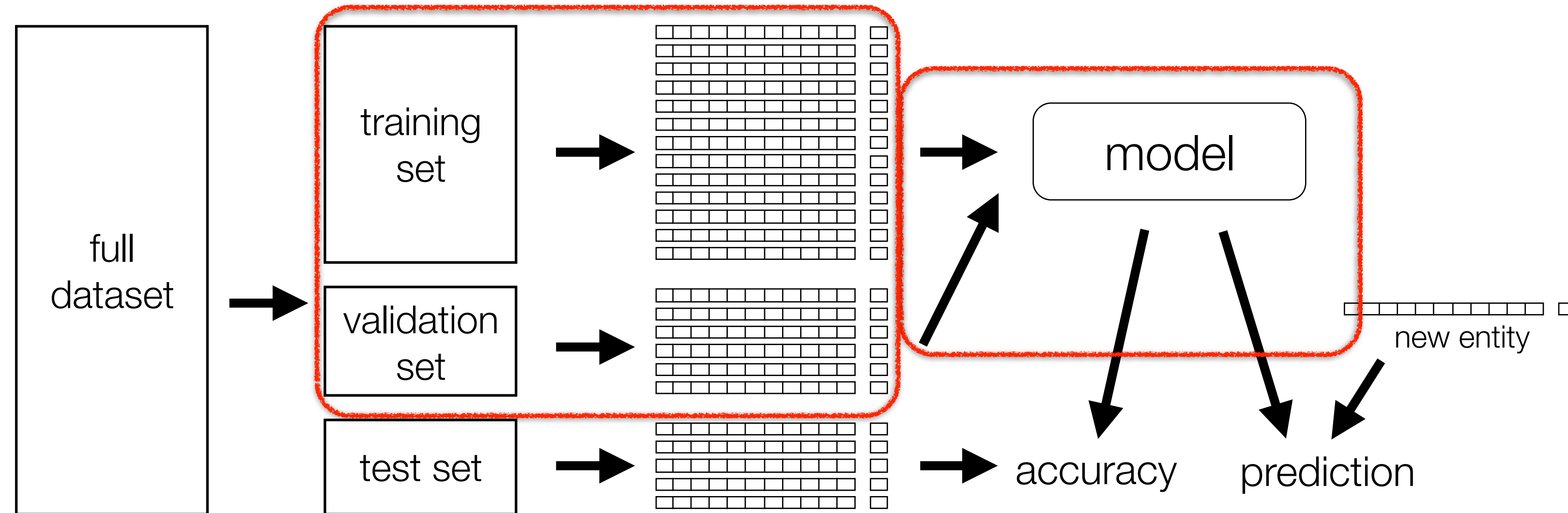




Supervised Learning: Logistic regression

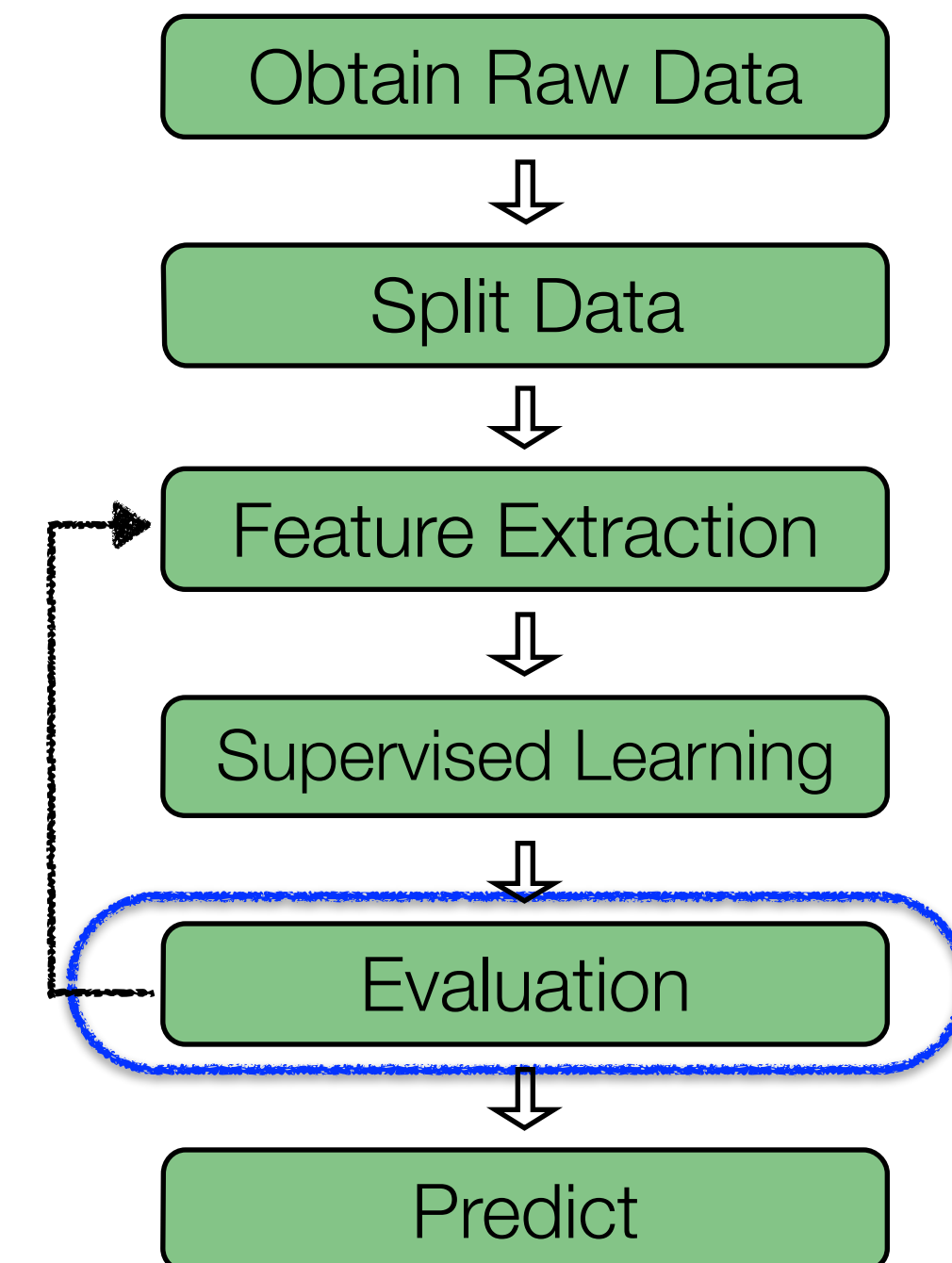
- Use MLlib implementation

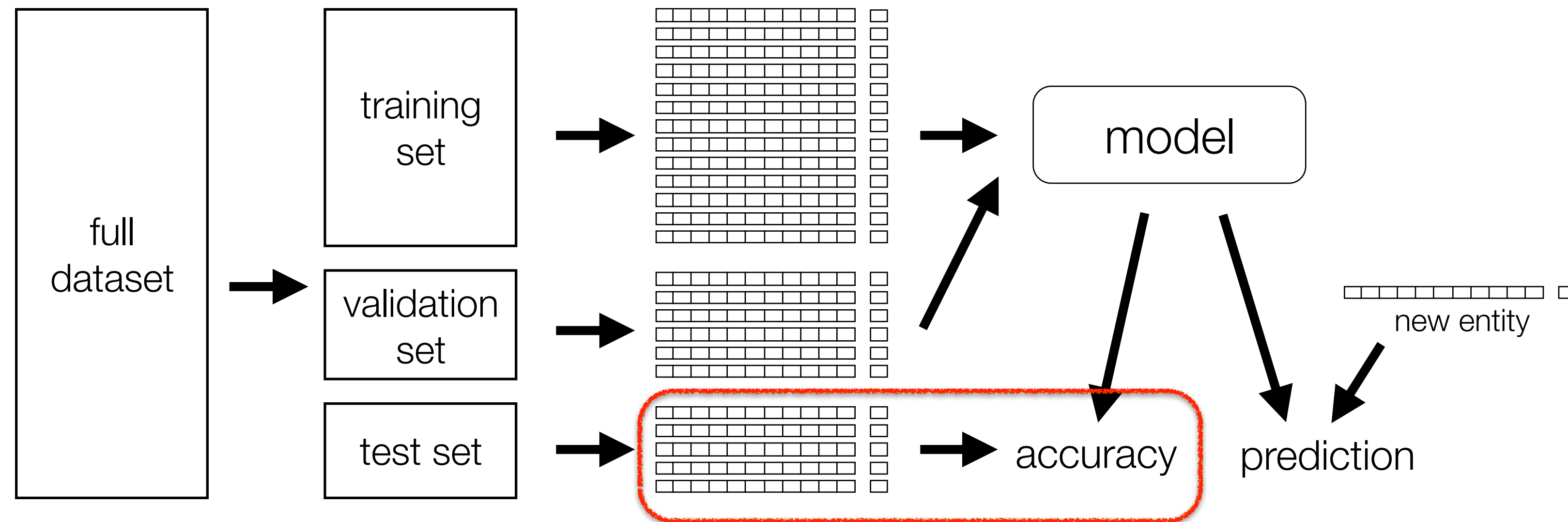




Evaluation (Part 1): Hyperparameter tuning

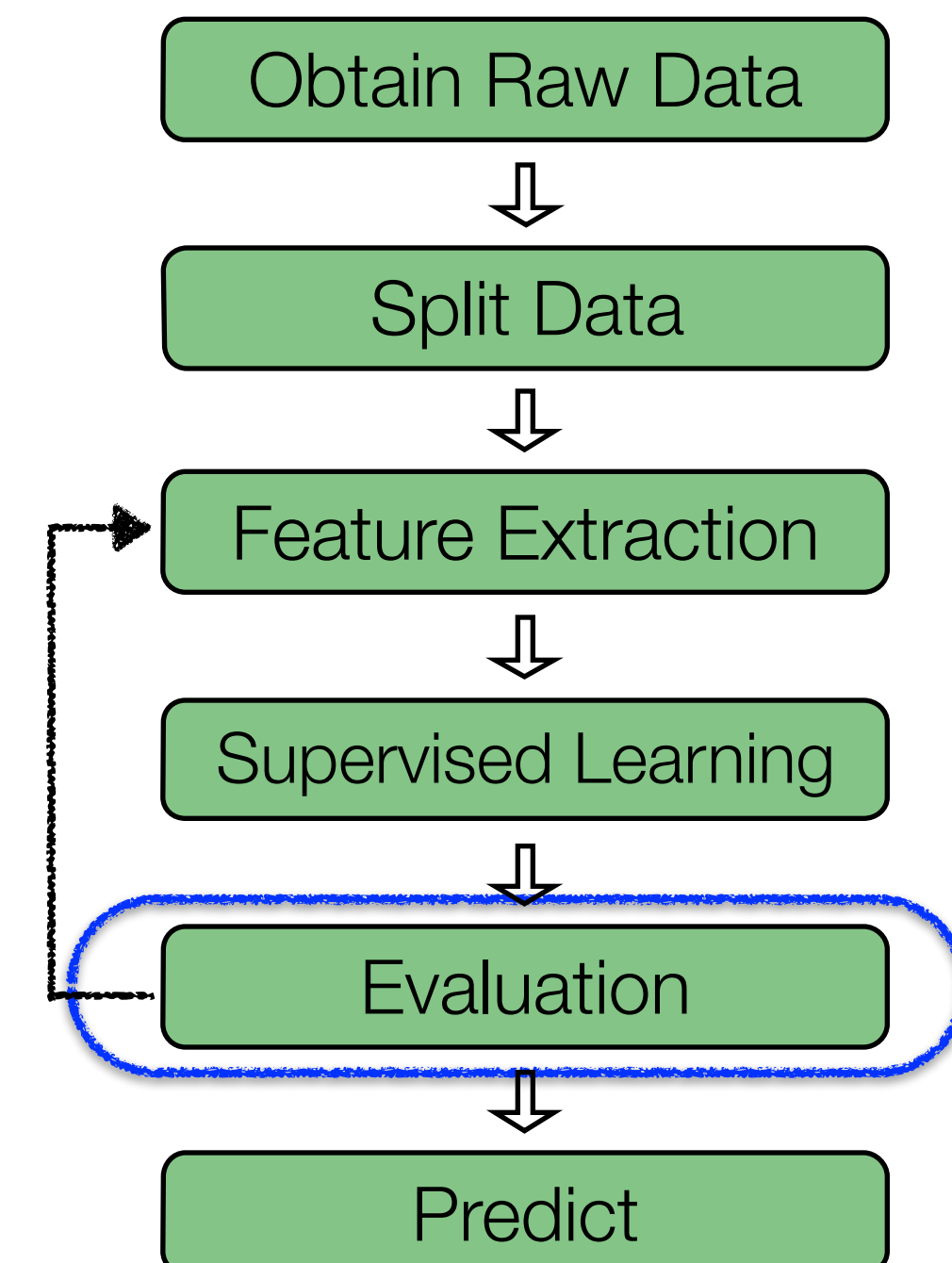
- Grid search to find good values for regularization
- Evaluate using logistic loss
- Visualize grid search
- Visualize predictions via ROC curve

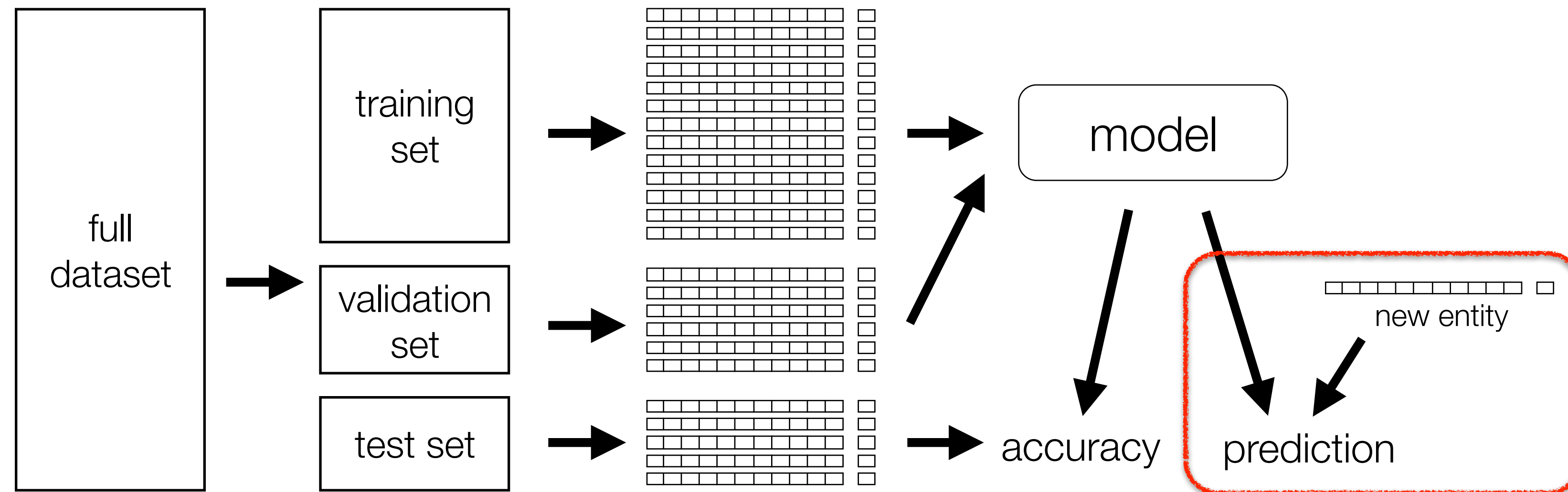




Evaluation (Part 2): Evaluate final model

- Evaluate using logistic loss
- Compare to baseline model (always predict value equal to the fraction of training points that correspond to click-through events)





Predict: Final model could be used to predict click-through rate for new user-ad tuple (we won't do this though)

