



# Introduction to Trigonometry with Applications

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APPLICATION EXAMPLE: ANALYSIS FOR ERROR IN POSITIONING OF TIP OF  
ONE-LINK ROBOT

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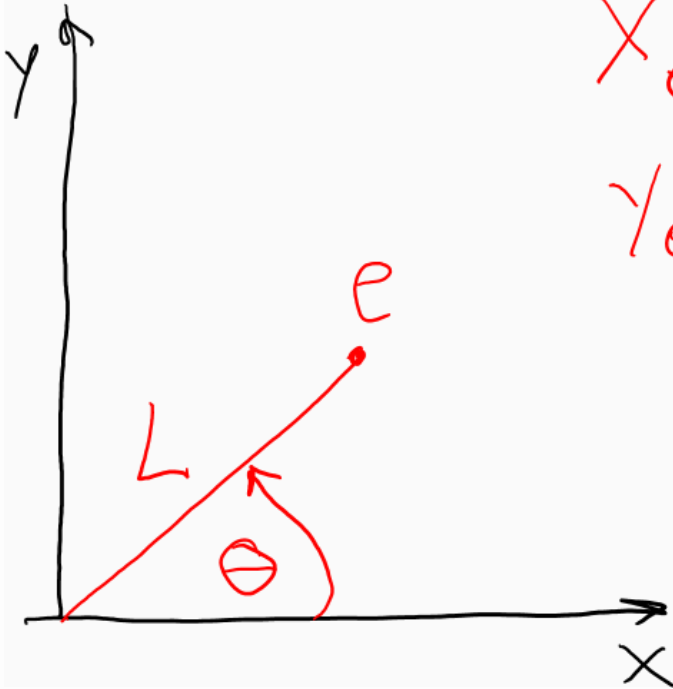


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## Application Example A: Analysis for Error in Positioning of Tip of One-Link Robot



$$x_e = L \cos(\theta)$$

$$y_e = L \sin(\theta)$$

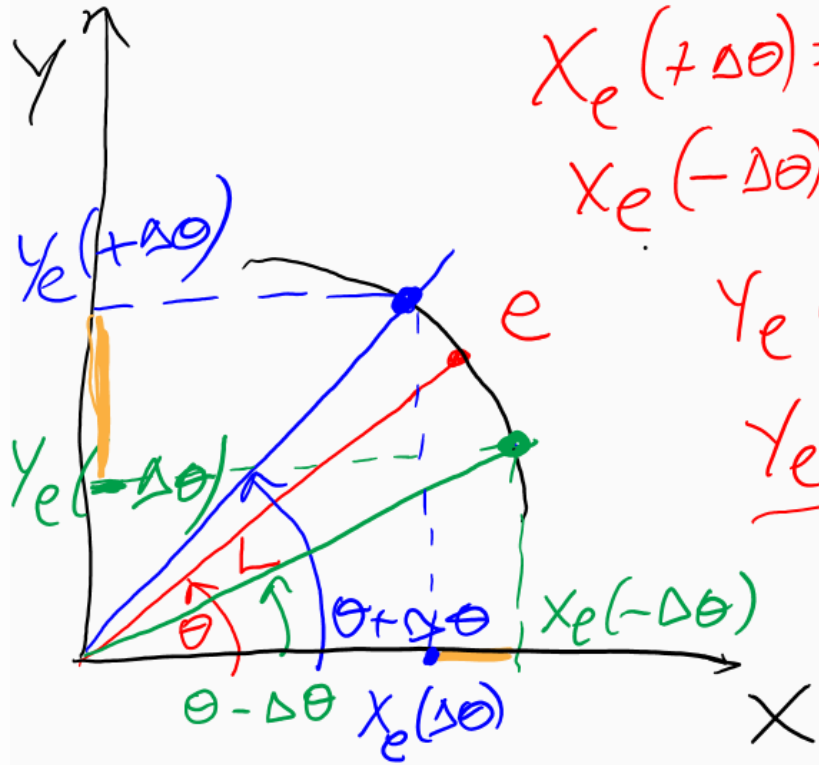
$\theta \rightarrow$  error  $\Delta\theta$ :  $\theta \pm \Delta\theta$

$$x_e = L \cos(\theta \pm \Delta\theta)$$

$$y_e = L \sin(\theta \pm \Delta\theta)$$



## Application Example B: Analysis for Error in Positioning of Tip of One-Link Robot



$$x_e(+\Delta\theta) = L \cos(\theta + \Delta\theta)$$

$$x_e(-\Delta\theta) = L \cos(\theta - \Delta\theta)$$

$$y_e(+\Delta\theta) = L \sin(\theta + \Delta\theta)$$

$$y_e(-\Delta\theta) = L \sin(\theta - \Delta\theta)$$

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$$L : 50 \text{ cm}$$

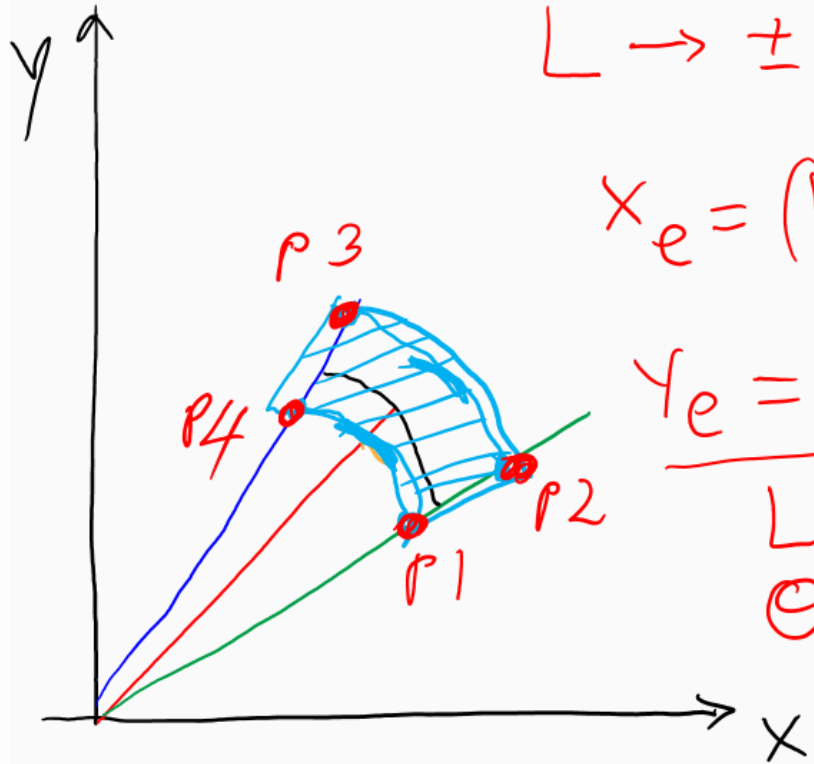
$$\Delta\theta : 0.5 \text{ degree}$$

$$\theta = 45^\circ$$



## Application Example C:

### Analysis for Error in Positioning of Tip of One-Link Robot



$$L \rightarrow \pm \Delta L \quad ; \quad \Theta \rightarrow \pm \Delta \Theta$$

$$x_e = (L \pm \Delta L) \cos(\Theta \pm \Delta \Theta)$$

$$y_e = (L \pm \Delta L) \sin(\Theta \pm \Delta \Theta)$$

$$L: 50 \text{ mm} \quad ; \quad \Delta L: 1 \text{ mm}$$

$$\Theta: 45^\circ \quad ; \quad \Delta \Theta = 0.5^\circ$$

$$P_1 \neq P_4 \quad ; \quad P_2 \neq P_3 \quad \begin{matrix} P_1 \neq P_2 \\ P_3 \neq P_4 \end{matrix}$$